

Name Key

a) Write a system of equations for the following word problem

"Small drinks cost \$1, medium drinks cost \$1.40, and large drinks cost \$2. A total of 24 drinks are bought and \$37.60 is spent. Twice as many large drinks as small drinks are bought."

$$\begin{aligned} S + M + L &= 24 \\ 1S + 1.4M + 2L &= 37.6 \\ -2S \quad \quad + L &= 0 \quad (\text{from } L = 2S) \end{aligned}$$

b) Solve the system to determine how many of each type of drink is bought.

To eliminate M:

-1.4 · row 1:

$$\begin{array}{r} -1.4S - 1.4M - 1.4L = -33.6 \\ 1S + 1.4M + 2L = 37.6 \\ \hline -1.4S \quad \quad -1.6L = 4 \\ -2S \quad \quad + L = 0 \end{array}$$

By subst., $L = 2S$

$$\begin{aligned} -1.4S + 1.6(2S) &= 4 \\ -1.4S + 3.2S &= 4 \\ 1.8S &= 4 \\ \frac{1.8S}{1.8} &= \frac{4}{1.8} \end{aligned}$$

$$\begin{aligned} S &= 5 \text{ small} \\ L &= 2 \cdot 5 = 10 \text{ large} \\ M &= 24 - 10 - 5 \\ &= 9 \text{ medium} \end{aligned}$$