

Origin symmetry

- reflected twice (about both x and y axes)
- replacing both x with -x and y with -y results in an equivalent equation
- An example:

$y = x^3$   
 Replace  
 $-y = (-x)^3 = -x^3$   
 $-y = -x^3$   
 $y = x^3$   
 Same  
 y-axis      x-axis



Ex c Test each equation for even, odd, and origin symmetry (it's possible there is no symmetry).

$y = 1/x$

y-axis  
 $y = \frac{1}{-x}$   
 no

x-axis  
 $-y = \frac{1}{x}$   
 no

origin  
 $\Delta y = \frac{1}{-x}$   
 $y = \frac{1}{x}$   
 yes

$y = x^2 + 2x + 4$

$y = (-x)^2 + 2(-x) + 4$   
 $y = x^2 - 2x + 4$   
 no

$-y = x^2 + 2x - 4$   
 no

$-y = x^2 - 2x + 4$   
 no

$y = x^4 + 2x^2$

$y = (-x)^4 + 2(-x)^2$   
 $= x^4 + 2x^2$   
 yes

no

no

$x^2 + y^2 = 9$

$(-x)^2 + y^2 = 9$   
 $x^2 + y^2 = 9$   
 yes

$x^2 + (-y)^2 \neq 9$   
 $x^2 + y^2 = 9$   
 yes

$(-x)^2 + (-y)^2 = 9$   
 $x^2 + y^2 = 9$   
 yes

$y = x^5$

$y = (-x)^5$   
 $y = -x^5$   
 no

$-y = x^5$   
 no

$-y = -x^5$   
 $y = x^5$   
 yes